

Rozdział 2 - NIERÓWNOŚCI KWADRATOWE

Lp.	Nierówność	Postać uproszczona	WYNIK
1	$x^2 - x > \frac{x}{2} + 1$	$2x^2 - 3x - 2 > 0$	$Z = \left(-\infty, -\frac{1}{2}\right) \cup \left(\frac{4}{3}, +\infty\right)$
2	$(2x+3)^2 < 1$	$x^2 + 3x + 2 < 0$	$Z = (-2, -1)$
3	$\left(\frac{1}{2}x + 1\right)^2 > 16$	$x^2 + 4x - 60 > 0$	$Z = (-\infty, -10) \cup (6, +\infty)$
4	$(3x-1)^2 - 4(2-x)^2 > 0$	$x^2 + 2x - 3 > 0$	$Z = (-\infty, -3) \cup (1, +\infty)$
5	$(1-3x)^2 + 3x - 4x^2 \geq 9$	$5x^2 - 3x - 8 \geq 0$	$Z = (-\infty, -1) \cup \left[\frac{8}{5}, +\infty\right)$
6	$(3x-2)^2 - x^2 - 2x \leq 1$	$8x^2 - 14x + 3 \leq 0$	$Z = \left[\frac{1}{4}, \frac{3}{2}\right]$
7	$2x^2 + 9 > (x-4)^2 + 14x$	$x^2 - 6x - 7 > 0$	$Z = \left(-\infty, -1\right) \cup \left(\frac{7}{2}, +\infty\right)$
8	$\sqrt{3}x^2 - 4x + \sqrt{3} < 0$		$Z = \left(\frac{\sqrt{3}}{3}, \sqrt{3}\right)$
9	$(x-1)^2 - 4 > 0$	$(x-3)(x+1) > 0$	$Z = \left(-\infty, -1\right) \cup \left(\frac{3}{2}, +\infty\right)$
10	$(2x+3)^2 - 1 < 0$	$(x+1)(x+2) < 0$	$Z = (-2, -1)$
11	$5(x+1) < x(3-x)$	$x^2 + 2x + 5 < 0$	$Z = \emptyset$
12	$x^2 - x \geq \frac{x}{2} + 1$	$2x^2 - 3x - 2 \geq 0$	$Z = \left(-\infty, -\frac{1}{2}\right) \cup \left[2, +\infty\right)$
13	$x(x-2) > 3(x-2)$	$x^2 - 5x + 6 > 0$	$Z = \left(-\infty, 2\right) \cup \left(\frac{3}{2}, +\infty\right)$
14	$(3x+2)^2 \leq 7(3x+2)$	$9x^2 - 9x - 10 \leq 0$	$Z = \left[-\frac{2}{3}, \frac{5}{3}\right]$
15	$(x-4)^2 + (x-4)(x+2) > 0$	$x^2 - 5x + 4 > 0$	$Z = \left(-\infty, 1\right) \cup \left(\frac{4}{3}, +\infty\right)$
16	$(x-3)^2 > (x-3)(2x+9)$	$-x^2 - 9x + 36 > 0$	$Z = (-12, 3)$
17	$-\frac{1}{2}(x+1)(x-3) \leq 0$	$x_1 = -1; x_2 = 3$	$Z = \left(-\infty, -1\right) \cup \left[3, +\infty\right)$
18	$-5(x-2)(1-x) \leq 0$	$x_1 = 2; x_2 = 1$	$Z = \langle 1, 2 \rangle$
19	$x^2 - 7 x + 10 \leq 0$		$Z = \langle -5, -2 \rangle \cup \langle 2, 5 \rangle$
20	$x^2 - 3 x - 4 \leq 0$		$Z = \langle -4, 4 \rangle$
21	$x^2 - 2x - 5 x-1 + 7 \leq 0$		$Z = \langle -2, -1 \rangle \cup \langle 3, 4 \rangle$
22	$x^2 - 4x + x-1 + 3 \leq 0$		$Z = \langle 1, 2 \rangle$
23	$ x^2 + 3x + 1 \leq 1$		$Z = \langle -3, -2 \rangle \cup \langle -1, 0 \rangle$
24	$ x^2 + 6x - 1 \leq 6$		$Z = \langle -7, -5 \rangle \cup \langle -1, 1 \rangle$
25	$-2x^2 + (x-1)^2 \leq -2$	$-x^2 - 2x + 3 \leq 0$	$Z = \left(-\infty, -3\right) \cup \left[1, +\infty\right)$

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26	$-x^2 - x + 2 > 0$		$Z = (-1, 1)$
27	$x^2 - 3 x + 2 \geq 0$		$Z = \langle -\infty, -2 \rangle \cup \langle -1, 1 \rangle \cup \langle 2, +\infty \rangle$
28	$x^2 - x \leq 0$		$Z = \langle -1, 1 \rangle$
29	$x^2 - 5x + 6 > 0$		$Z = (-\infty, -3) \cup \langle -2, -1 \rangle \cup \langle 6, +\infty \rangle$
30	$ x^2 - 3 < 1$		$Z = (-2, -\sqrt{2}) \cup (\sqrt{2}, 2)$
31	$\frac{5x^2 + 9}{6} - \frac{4x^2 - 9}{5} > 3$	$x^2 + 9 > 0$	$Z = \mathbb{R}$
32	$x - 8 < 3x < 15 + x - x^2$		$Z = (-4, 3)$
33	$2 < x^2 - x < x^2 + 2x$		$Z = \langle 0, +\infty \rangle$
34	$x^2 - 11 < 5x + 3 < 7 + 9x$		$Z = (-1, 7)$
35	$x^2 + 2x - 8 \leq 3x - 8$	$x(x-1) \leq 0$	$Z = \langle 0, 1 \rangle$
36	$-x^2 + 6x - 6 \leq 3x - 3$	$-x^2 + 3x - 3 \leq 0; \Delta = -3$	$Z = \mathbb{R}$
37	$2x^2 + 19 > 8x + 8$	$2x^2 - 8x + 11 > 0; \Delta = -24$	$Z = \mathbb{R}$
38	$4x - 8 \geq -x^2 + 5x - 2$	$x^2 - x - 6 \geq 0$	$Z = \langle -\infty, -2 \rangle \cup \langle 3, +\infty \rangle$
39	$x^2 + 6x + 9 \leq 0$	$(x+3)^2 \leq 0$	$Z = \{-3\}$